# Higher-Ranked Exception Types

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Exception Types
In Haskell "types do not lie":
Functions behave as mathematical function on the domain and range given by their type

#### Higher-Ranked Exception Types

The problem is that we have already committed the first argument of *map* to be of type

- Side-effects are made explicit by monadic types
  Exceptions that may be raised are *not* captured in the type
- We would like them to be during program verificationAdding exception types to Haskell is more complicated
- than in a strict first-order language

### Exception Types in Haskell

- Exception types in Haskell can get complicated because of:
- Higher-order functions Exceptions raised by higher-order functions depend on the exceptions raised by functional arguments. Non-strict evaluation Exceptions are not a form of control flow, but are values that can be embedded inside other values. • An exception-annotated type for *map* would be:  $map : \forall \alpha \ \beta \ e_1 \ e_2 \ e_3 \ e_4.$  $(\alpha^{e_1} \xrightarrow{e_3} \beta^{(e_1 \cup e_2)}) \xrightarrow{\oslash} [\alpha^{e_1}]^{e_4} \xrightarrow{\oslash} [\beta^{(e_1 \cup e_2 \cup e_3)}]^{e_4}$  $map = \lambda f.\lambda xs.$  case xs of  $[] \mapsto []$  $(y: ys) \mapsto f \ y: map \ f \ ys$

 $\alpha^{e_1} \xrightarrow{e_3} \beta^{(e_1 \cup e_2)}$ 

- It always propagates exceptional values from the input to the output
- The solution is to move from Hindley–Milner to System  $F_{\omega}$ , introducing *higher-ranked exception types* and *exception operators* 
  - $\begin{array}{ll} map & : \forall e_2 \ e_3.(\forall e_1.\alpha^{e_1} \xrightarrow{e_3} \beta^{(e_2 \ e_1)}) \\ & \to (\forall e_4 \ e_5.[\alpha^{e_4}]^{e_5} \to [\beta^{(e_2 \ e_4 \ \cup \ e_3)}]^{e_5}) \\ id & : \forall e.\alpha^{e} \xrightarrow{\oslash} \alpha^{e} \\ const \ \bot_{\mathbf{E}} : \forall e.\alpha^{e} \xrightarrow{\oslash} \beta^{\{\mathbf{E}\}} \end{array}$
- ► This gives us the desired exception types: *map id* :  $\forall e_4 \ e_5 . [\alpha^{e_4}]^{e_5} \rightarrow [\alpha^{e_4}]^{e_5}$ *map* (const  $\perp_{\mathbf{E}}$ ):  $\forall e_4 \ e_5 . [\alpha^{e_4}]^{e_5} \rightarrow [\beta^{\{\mathbf{E}\}}]^{e_5}$

## Precise Exception Types

The exception type above is not a precise as we

# Exception Type Inference

- Higher-ranked exception types are syntactically heavy; we need type inference
- Type inference is undecidable in System F<sub>w</sub>, but exception types piggyback on an underlying type
  Holdermans and Hage (2010) show that type inference is decidable for a similar higher-ranked annotated type system with type operators

#### Work-in-Progress

Imprecise exception semantics Haskell has an *imprecise exception semantics* 

#### would like

 $\begin{array}{l} \text{map id} & : [\alpha^{e_1}]^{e_4} \to [\alpha^{e_1}]^{e_4} \\ \text{map } (\text{const } \bot_{\mathbf{E}}) : [\alpha^{e_1}]^{e_4} \to [\beta^{(e_1 \cup \{\mathbf{E}\})}]^{e_4} \end{array}$ 

A more appropriate type for map (const  $\perp_E$ ) would be:

 $map (const \perp_{\mathbf{E}}) : [\alpha^{e_1}]^{e_4} \to [\beta^{\{\mathbf{E}\}}]^{e_4}$ 

Exceptional elements in the input list cannot be propagated to the output. Needed for soundness of various program transformations in an optimizing compiler
Not adequately captured by ACI1 constraints; attempt to use equational unification in Boolean rings instead
Metatheory Is the combined rewrite system of STLC and BR still confluent and normalizing?
Needed for decidable exception type equality
Hope to use a general result by Breazu-Tannen